

# Model Question Paper

Subject: → Refrigeration and air conditioning

Question 1: → The temperature limits of an ammonia refrigerating system are  $25^{\circ}\text{C}$  and  $-10^{\circ}\text{C}$ . If the gas is dry at the end of compression, calculate 1) Draw T-S and P-H diagram and 2) calculate COP of the cycle assuming no undercooling of the liquid ammonia. Use the following table for properties of ammonia

Temperature ( $^{\circ}\text{C}$ )	liquid heat ( $\frac{\text{kJ}}{\text{kg}}$ )	latent heat ( $\frac{\text{kJ}}{\text{kg}}$ )	liquid entropy ( $\frac{\text{kJ}}{\text{kg}}$ )
25	298.9	1166.94	1.1292
-10	135.37	1297.68	0.5943

Question 2: → An aircraft refrigeration plant has to handle a cabin load of 30 tonnes. The atmospheric temperature is  $17^{\circ}\text{C}$ . The atmospheric air is compressed to a pressure of 0.95 bar and temperature of  $30^{\circ}\text{C}$  due to ram action. This air is then further compressed in a compressor to 4.75 bar, cooled in a heat exchanger to  $6^{\circ}\text{C}$ , expanded in a turbine to 1 bar pressure and supplied to the cabin. The air leaves the cabin at a temperature of  $27^{\circ}\text{C}$ . The isentropic efficiencies of both compressor and turbine are 0.9. Calculate the mass of air circulated per minute and COP. For air  $c_p = 1.004 \text{ kJ/kgK}$  and  $\gamma = 1.4$

Question 3: → Derive an expression for COP of an ideal vapour absorption system in terms of temperature  $T_1$  at which heat is supplied to the generator, the temp<sup>r</sup>

$T_e$  at which heat is absorbed in the evaporator and the temperature  $T_c$  at which heat is discharged from the condenser and absorber.

Question 4  $\rightarrow$  The humidity ratio of atmospheric air at  $28^\circ\text{C}$  dry bulb temp<sup>o</sup> and 760 mm of mercury is  $0.016 \text{ kg/kg}$  of dry air.

Determine 1) Partial pressure of water vapour

2) Relative humidity

3) Dew point temp<sup>o</sup>

4) Specific enthalpy and

5) Vapour density

Question 5  $\rightarrow$  A small office hall of 25 persons capacity is provided with summer air conditioning with following data

outside conditions =  $34^\circ\text{C}$  DBT and  $28^\circ\text{C}$  WBT

Inside conditions =  $24^\circ\text{C}$  DBT and 50% RH

Volume of air supplied =  $0.4 \text{ m}^3/\text{min}/\text{person}$

Sensible heat load in room =  $125600 \text{ kJ/h}$

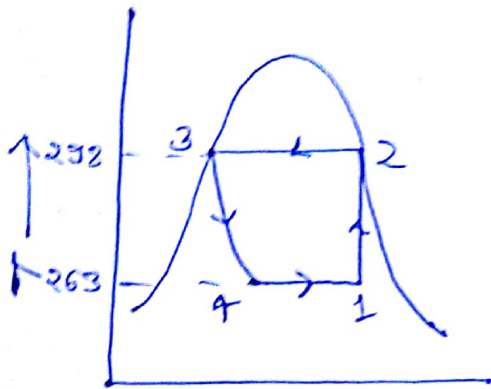
Latent heat load in room =  $42000 \text{ kJ/h}$

Find sensible heat factor of the plant.

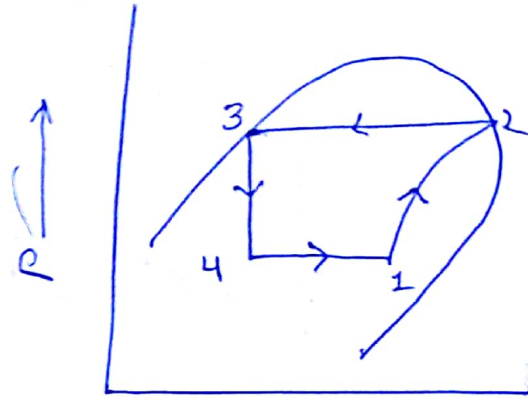
# Solution of Model Question Paper

Subject: → Refrigeration and air conditioning

Answer 1: → 1) T-s and P-h diagrams are



S →



h →

2) we know that entropy at point 1

$$S_1 = S_{f1} + \frac{x_1 h_{fg1}}{T_1} = 0.5443 + \frac{x_1 \times 1297.68}{263}$$

$$= 0.5443 + 4.939x_1$$

Similarly at point 2

$$S_2 = S_{f2} + \frac{h_{fg2}}{T_2} = 1.1242 + \frac{1166.94}{298} = 5.04$$

we know  $S_1 = S_2$

$$0.5443 + 4.934x_1 = 5.04 \Rightarrow x_1 = 0.91$$

enthalpy at point 1

$$h_1 = h_{f1} + x_1 h_{fg1} = 135.37 + 0.91 \times 1297.68 = 1316.26 \text{ kJ/kg}$$

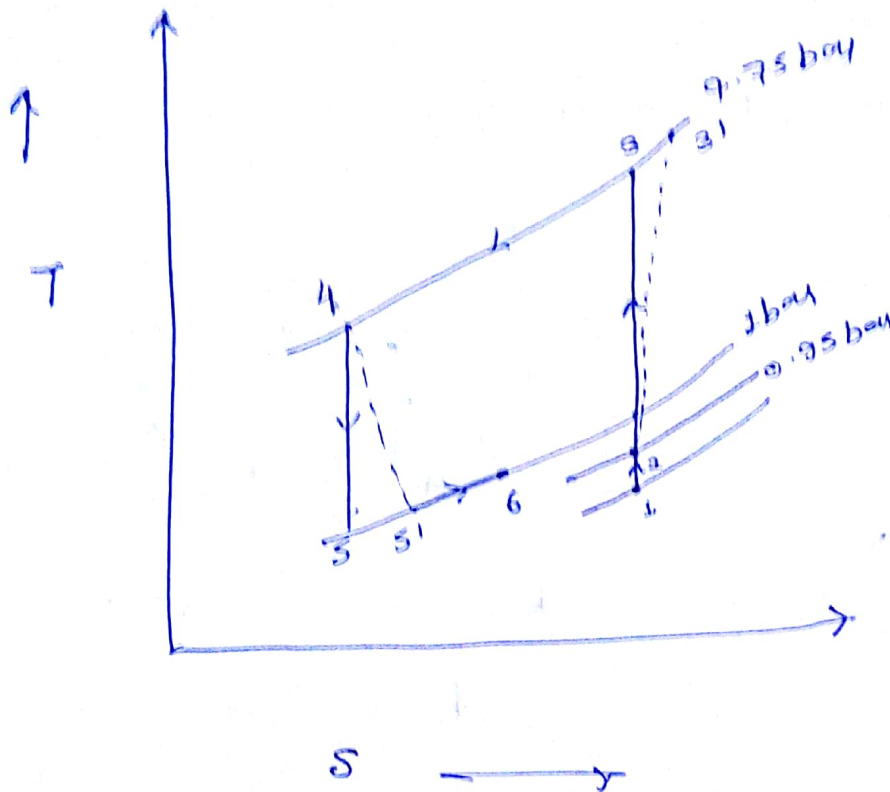
$$h_2 = h_{f2} + h_{fg2} = 298.9 + 1166.94 = 1465.84 \text{ kJ/kg}$$

$$\text{COP} = \frac{h_1 - h_{f3}}{h_2 - h_1}$$

$$= \frac{1316.26 - 298.9}{1465.84 - 1316.26} = 6.8$$

$$\boxed{\text{COP} = 6.8}$$

Solution 2 The T-s diagram for simple air conditioning is



$T_3$  = Temp<sup>r</sup> of the air after isentropic compression in the compressor  
 $T_3'$  = Actual temp<sup>r</sup> of the air leaving the compressor  
 $T_5$  = Temp<sup>r</sup> of the air leaving the turbine after isentropic expansion  
 $T_5'$  = Actual temp<sup>r</sup> of air leaving the turbine

isentropic compression in process 2-3

$$\frac{T_3}{T_2} = \left(\frac{P_3}{P_2}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{4.75}{0.95}\right)^{\frac{1.4-1}{1.4}} = 1.584$$

$$T_3 = T_2 \times 1.584 = 303 \times 1.584 = 480 \text{ K}$$

and efficiency of compressor

$$\eta_c = \frac{\text{Isentropic increase in temp}^r}{\text{Actual increase in temp}^r} = \frac{T_3 - T_2}{T_3' - T_2}$$

$$0.9 = \frac{480 - 303}{T_3' - 303} = \frac{177}{T_3' - 303}$$

$$T_3' = 499.7 \text{ K}$$

efficiency of turbine

$$\eta_T = \frac{\text{Actual increase in temp}^\circ}{\text{Isentropic increase in temp}^\circ} = \frac{T_H - T_5'}{T_H - T_5}$$

isentropic expansion in process 4-5

$$\frac{T_4}{T_5} = \left(\frac{P_4}{P_5}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{11.75}{1}\right)^{\frac{1.4-1}{1.4}} = 1.561$$

$$T_5 = 340/1.561 = 217.8 \text{ K}$$

$$\eta_T = \frac{T_H - T_5'}{T_H - T_5} \Rightarrow 0.9 = \frac{340 - T_5'}{340 - 217.8}$$

$$T_5' = 230 \text{ K}$$

mass of air circulated

$$m_a = \frac{210 \text{ Q}}{c_p(T_6 - T_5)} = \frac{210 \times 30}{1.004(300 - 230)} = 89.64 \text{ kg/min}$$

$$\text{COP} = \frac{210 \text{ Q}}{m_a c_p (T_2' - T_2)} = \frac{210 \times 30}{89.64 \times 1.004 (499.7 - 303)} = 0.356$$

Solution 3: → Given

$T_G$  = Temp<sup>o</sup> at which heat is supplied to generator

$T_E$  = Temp<sup>o</sup> at which heat is absorbed in evaporator

$T_C$  = Temp<sup>o</sup> at which heat is discharged from condenser and absorber.

we know that

$$Q_C = Q_G + Q_E$$

and we know that initial entropy is equal to the entropy after change in condition.

$$\frac{Q_G}{T_G} + \frac{Q_E}{T_C} = \frac{Q_C}{T_C}$$

$$= \frac{Q_G + Q_E}{T_C}$$

$$\frac{Q_G}{T_G} - \frac{Q_G}{T_C} = \frac{Q_E}{T_C} - \frac{Q_E}{T_E}$$

$$Q_G \left( \frac{T_C - T_G}{T_G \times T_C} \right) = Q_E \left( \frac{T_E - T_C}{T_E \times T_C} \right)$$

$$Q_G = Q_E \left[ \frac{T_E - T_C}{T_C \times T_E} \right] \left[ \frac{T_G \times T_C}{T_C - T_G} \right]$$

$$= Q_E \left( \frac{T_C - T_E}{T_E} \right) \left( \frac{T_G}{T_G - T_C} \right)$$

$$(COP)_{max} = \frac{Q_E}{Q_G} = \frac{Q_E}{Q_E \left( \frac{T_C - T_E}{T_E} \right) \left( \frac{T_G}{T_G - T_C} \right)}$$

$$(COP)_{max} = \left( \frac{T_E}{T_C - T_E} \right) \left( \frac{T_G - T_C}{T_G} \right)$$

Solution 4 →

Given →  $t_d = 28^\circ$   $P_b = 760 \text{ mm of Hg}$   $W = 0.016 \text{ kg/kg of dry}$

1) Partial Pressure of water vapour

$P_v$  = Partial p<sup>r</sup> of water vapour

we know humidity Ratio (W)

$$W = \frac{0.622 P_v}{P_b - P_v} \Rightarrow 0.016 = \frac{0.622 P_v}{760 - P_v}$$

$$P_v = 19.06 \text{ mm of Hg}$$

$$= 2540.6 \text{ N/m}^2$$

2) Relative humidity

From steam table, we find that the saturation p<sup>o</sup> of Vapour corresponding to dry bulb temp<sup>o</sup> of 28°C is

$$P_s = 0.03778 \text{ bar} = 3778 \text{ N/m}^2$$

Relative humidity

$$\phi = \frac{P_v}{P_s} = \frac{2540.6}{3778} = 0.672 = 67.2\%$$

3) Dew point temp<sup>o</sup>

from steam table for  $P_v = 2540.6$

$$t_{dp} = 21.1^\circ\text{C}$$

4) Specific enthalpy

from steam table  $t_{dp} = 21.1^\circ\text{C}$

$$h_{fgdp} = 2451.76 \text{ kJ/kg}$$

$$h = 1.022 t_d + w (h_{fgdp} + 2.3 t_{dp})$$

$$= 1.022 \times 28 + 0.016 (2451.76 + 2.3 \times 21.1)$$

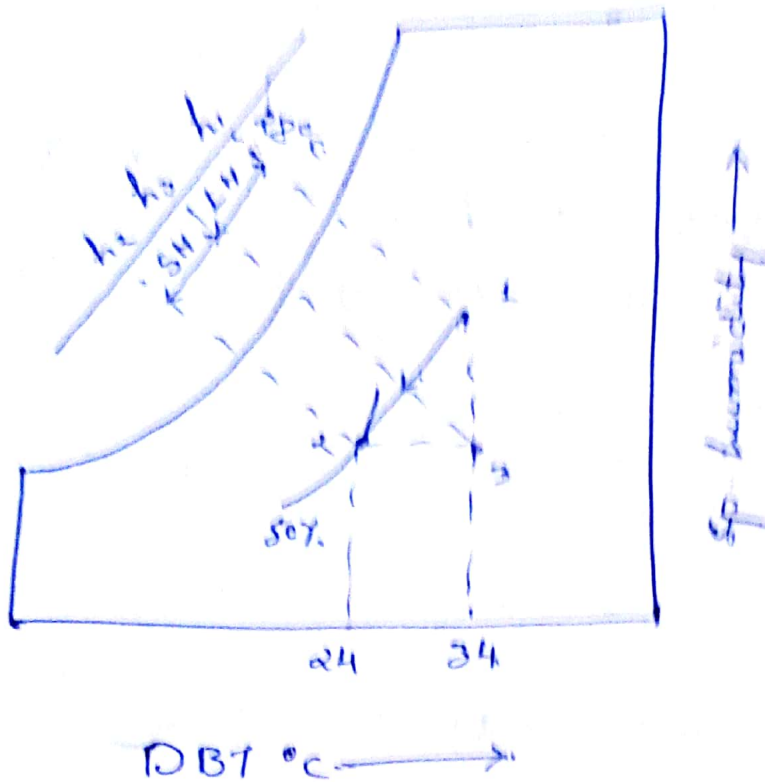
$$= 68.62 \text{ kJ/kg of dry air}$$

5) Vapour density

$$P_v = \frac{w (P_b - P_v)}{R_a T_d} = \frac{0.016 (760 - 19.06) 133.3}{287 (273 + 28)}$$

$$= 0.0183 \text{ kg/m}^3 \text{ of dry air}$$

Solution 5 →



from the psychrometric chart

$V_{s1}$  (specific volume) =  $0.9 \text{ m}^3/\text{kg}$  of dry air

$h_1$  (Enthalpy at 1) =  $90 \text{ kJ/kg}$  of dry air

$h_2$  ( " " 2 ) =  $48 \text{ kJ/kg}$  " " "

$h_3$  ( " " 3 ) =  $58 \text{ kJ/kg}$  " " "

mass of air supplied

$$m_a = \frac{V_1}{V_{s1}} = \frac{10}{0.9} = 11.1 \text{ kg/min}$$

Sensible heat removed from the air

$$= m_a (h_3 - h_2) = 11.1 (58 - 48)$$

$$= 111 \text{ kJ/min} = 6660 \text{ kJ/h}$$



Total sensible heat of room

$$\begin{aligned}SH &= 6660 + 125600 \\ &= 132260 \text{ kJ/h.}\end{aligned}$$

Latent heat from air

$$\begin{aligned}&= m_a (h_1 - h_2) \\ &= 11.1 (90 - 58) \\ &= 355 \text{ kJ/min} = 21300 \text{ kJ/h.}\end{aligned}$$

Total latent heat

$$\begin{aligned}LH &= 21300 + 42000 \\ &= 63300 \text{ kJ/h}\end{aligned}$$

Sensible heat factor

$$SHF = \frac{SH}{SH+LH} = \frac{132260}{132260 + 63300}$$

$$\boxed{SHF = 0.676}$$